

$$\lim_{x \rightarrow \infty} \left[ \sqrt[3]{x^2(2-x)} + x \right] = (-\infty + \infty) = \text{ROZŠÍŘIT}$$

$$= \lim_{x \rightarrow \infty} \left( \sqrt[3]{x^2(2-x)} + x \right) \cdot \frac{\left[ x^2(2-x) \right]^{\frac{2}{3}} - \left[ x^2(2-x) \right]^{\frac{1}{3}} \cdot x + x^2}{\left[ x^2(2-x) \right]^{\frac{2}{3}} - \left[ x^2(2-x) \right]^{\frac{1}{3}} \cdot x + x^2}$$

POZNÁMKA:  $\left( (a+b) \cdot \left( \frac{a^2-ab+b^2}{a^2-ab+b^2} \right) = \frac{a^3+b^3}{a^2-ab+b^2} \right) \leftarrow$  VZOREC

$$= \lim_{x \rightarrow \infty} \frac{x^2(2-x) + x^3}{\left[ x^2(2-x) \right]^{\frac{2}{3}} - \left[ x^2(2-x) \right]^{\frac{1}{3}} \cdot x + x^2} =$$

VYTKNEME  $x^2$

$$= \lim_{x \rightarrow \infty} \frac{2x^2 - x^3 + x^3}{x^2 \left[ \left( \frac{2}{x} - 1 \right)^{\frac{2}{3}} - \left( \frac{2}{x} - 1 \right)^{\frac{1}{3}} + 1 \right]} =$$

$$= \lim_{x \rightarrow \infty} \frac{2x^2}{x^2} \cdot \frac{1}{\left( \frac{2}{x} - 1 \right)^{\frac{2}{3}} - \left( \frac{2}{x} - 1 \right)^{\frac{1}{3}} + 1} =$$

$$= \frac{2}{(-1)^{\frac{2}{3}} + 1 + 1} = \frac{2}{3}$$

POUŽITÝ VZOREC

$$(a+b)(a^2-ab+b^2) = a^3+b^3$$

$$\lim_{x \rightarrow -\infty} \left[ \sqrt[3]{x^2(2-x)} + x \right] = (\infty - \infty) \dots \text{STEJNÝ POSTUP}$$