

2) ověřte přímým výpočtem pro 1atomový plyn $C_v = \frac{1}{kT^2} \langle E^2 \rangle$

$$C_v = \left(\frac{\partial E}{\partial T} \right)_N = \left| E = \frac{3}{2} kT \right| = \underline{\underline{\frac{3}{2} k}}$$

$$C_v = \frac{1}{kT^2} \langle E^2 \rangle = \frac{1}{kT^2} (\langle E^2 \rangle - \langle E \rangle^2) = \frac{1}{kT^2} (\langle E^2 \rangle - \frac{9}{4} k^2 T^2)$$

$$\begin{aligned} \langle E^2 \rangle &= \sum_n E_n^2 w_n = \sum_n E_n^2 \frac{1}{Z} e^{-\frac{E_n}{kT}} = \sum_n E_n^2 \frac{e^{-\frac{E_n}{kT}}}{\sum_n e^{-\frac{E_n}{kT}}} = \left| E_n = \frac{3}{2} kT \right| = \\ &= \frac{9}{4} k^2 T^2 \cdot \underbrace{\sum_n \frac{e^{-\frac{3}{2}}}{\sum_n e^{-\frac{3}{2}}}}_1 = \frac{9}{4} k^2 T^2 \Rightarrow C_v = 0 \end{aligned}$$

muselo by platit $\langle E^2 \rangle = \frac{15}{4} k^2 T^2$ ale nevím jak na to dojít